

### **Union by Size**

# **Learning Objectives**

1. Know the runtime of find after unioning by size



# **Union by Size**

To show that every tree in a disjoint set data structure using union by size has a height of at most O(log n) we will show that the inverse.

**Base Case** 

Inductive Hypothesis



## Case 1: r is taller than s

r - root tree

s - smaller tree

r' - resulting tree







## Case 2: r is shorter than s

r - root tree

s - smaller tree

r' - resulting tree





